Chapter 6, Hash tables:

- General introduction; separate chaining (Today)
- Practice open addressing (Thursday lab)
- Open addressing (Friday)
- Hash functions (next week Monday)
- Perfect hashing (week-after Monday)
- Hash table performance (week-after Wednesday)

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Today:

- Test problems
- The story of the Map ADT
- Goals and terminology of the unit
- Separate chaining implementation
- Variables and metrics of performance

Find	Search the data structure for a given key
Insert	Add a new key to the data structure
Delete	Get rid of a key and fix up the data structure

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containsKey() Find

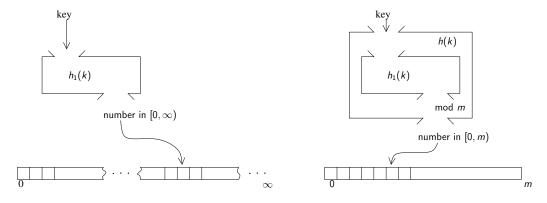
get() Find

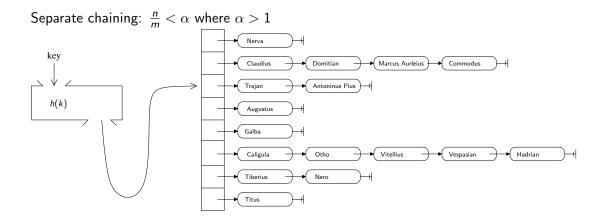
put() Find + insert

remove() Find + delete

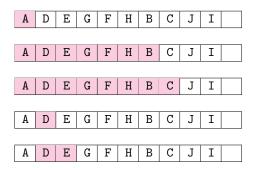
	Find	Insert	Delete
Unsorted array	$\Theta(n)$	$\Theta(1) \ [\Theta(n)]$	$\Theta(n)$
Sorted array	$\Theta(\lg n)$	$\Theta(n)$	$\Theta(n)$
Linked list	$\Theta(n)$	$\Theta(1)$	$\Theta(1)$
Balanced BST	$\Theta(\lg n)$	$\Theta(1) \ [\Theta(\lg n)]$	$\Theta(1) \ [\Theta(\lg n)]$
What we want	$\Theta(1)$	$\Theta(1)$	$\Theta(1)$

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Open addressing: $\frac{n}{m} < \alpha$ where $\alpha < 1$



Α	D	Е	G	F	H	В	С	J	I	
A	D	Е	G	F	H	В	С	J	I	
A	D	Е	G	F	H	В	С	J	I	
А	D	Е	G	F	Η	В	С	J	Ι	
A	D	Е	G	F	H	В	С	J	Ι	

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Unit agenda:

Solution 1: Separate chaining (plus basic concepts and terminology). (Today and lab)

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- Solution 2: Open addressing. (Friday)
- All about hash functions. (next week Monday)
- Solution 3: Perfect hashing. (week-after Monday)
- Looking carefully at performance. (week-after Wednesday)

Hash table terminology:

- ▶ Hash table: A *data structure*, not an ADT
- Bucket: A position in the (main) array, or, abstractly, an index in the range [0, m].
- ► Hash function: A function from keys to buckets.
- ► Collision: When two keys are hashed to the same bucket.
- Chain: A sequence of keys that needs to be searched through to find a given key.

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• Load factor (α): An upper bound on the ratio of keys to buckets.

Factors in best vs worst vs expected case:

- State of the table
- Length of the bucket
- Position of key in the bucket.

Parameters that can be adjusted for engineering a hash table:

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- \blacktriangleright Load factor α
- Rehash strategy
- Hash function

$$\begin{array}{cccc} O(1) & c_{0} \\ O(1) & c_{0} \\ O(1) & c_{0} \\ \vdots \\ O(1) & c_{0} \end{array} \end{array} \right\} \begin{array}{c} T(n) &= (n-1)c_{0} + c_{1} + c_{2}n \\ &= (c_{0} + c_{2})n + c_{1} - c_{0} \\ &= \Theta(n) \\ \vdots \\ O(1) & c_{0} \end{array} \right\}$$

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Hash functions should distribute the keys *uniformly* and *independently*.

Uniformity:

$$P(h(k)=i)=\frac{1}{m}$$

Independence:

$$P(h(k_1) = i) = P(h(k_1) = i | h(k_2) = j)$$

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Coming up:

Do Optimal BST project (Due Mon, Nov 25)

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Due **Wed, Nov 20** (end of day) Read Sections 7.(1 & 2) Take quiz (actually due Thurs, Nov 21)

Due **Fri, Nov 22** (end of day) Read Section 7.3 Do Exercises 7.(4,5,7,8) Take quiz