

1. Write a function `leastSigDigs` that takes a list of ints and returns a list of the least significant digits in those lists. For example, `leastSigDigs([283, 7234, 5, 2380])` would return `[3, 4, 5, 0]`.

```
fun leastSigDigs([]) = []
  | leastSigDigs(x::rest) = (x mod 10)::leastSigDigs(rest);
```

2. Write a function `hasEmpty` that takes a list of lists (of any type) and determines whether or not the list of lists contains an empty list. For example, `hasEmpty([[1,2,3], [4,5], [], [6,7]])` would return `true`.

```
fun hasEmpty([]) = false
  | hasEmpty([]::rest) = true
  | hasEmpty(x::rest) = hasEmpty(rest);
```

3. Use quantified syllogisms (and, possible, common syllogisms and logical equivalences) to verify the following argument form. (Note that $x \notin A$ is the same thing as $\sim (x \in A)$.) (11 points.)

- a. $\forall x \in A, P(x) \vee Q(x)$
- b. $\forall x \in A, P(x) \rightarrow R(x)$
- c. $\forall x \in A, Q(x) \rightarrow x \in B$
- d. $\forall x \in B, x \notin A \vee R(x)$
- e. $\therefore \forall x \in A, R(x)$

Suppose $a \in A$

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|-------|------------------------------------|--|
| (i) | $P(a) \vee Q(a)$ | By supposition, (a), and UI |
| | Suppose $P(a)$ | |
| (ii) | $R(a)$ | By supposition, (b), and UMP |
| | Suppose $Q(a)$ | |
| (iii) | $x \in B$ | By supposition, (c), and UMP |
| (iv) | $R(a)$ | By supposition, (iii), and elimination |
| (v) | $R(a)$ | By (ii), (iv), supposition, and HDC |
| (vi) | $\therefore \forall x \in A, R(x)$ | |