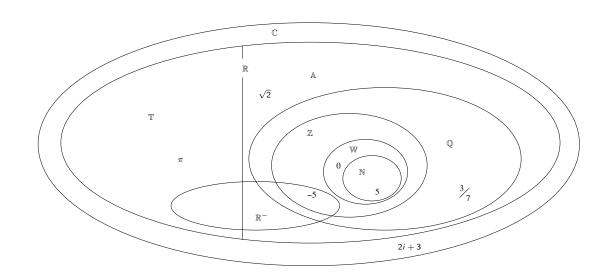
Chapter 1 outline:

- Introduction, sets and elements (this past Wednesday)
- Set operations; visual verification of set propositions (Today)
- Introduction to SML; cardinality and Cartesian products (Monday)
- Making types and functions in SML (Wednesday)
- ▶ More about functions in SML; introduction to lists [Chapter 2] (Next-week Friday)

Today:

- Set symbols and terminology
- Set notation
- Set operations
- Verifying set equivalence visually



5 is a natural number; or the collection of natural numbers contains 5. $5 \in \mathbb{N}$

Adding 0 to the collection of natural numbers makes the collection of $\mathbb{N} \cup \{0\} = \mathbb{W}$ whole numbers.

Merging the algebraic numbers and the transcendental numbers makes $\mathbb{A} \cup \mathbb{T} = \mathbb{R}$ the real numbers.

Transcendental numbers are those real numbers which are not algebraic $\mathbb{T} = \mathbb{R} - \mathbb{A}$ numbers.

Nothing is both transcendental and algebraic, or the collection of things $\mathbb{T} \cap \mathbb{A} = \emptyset$ both transcendental and algebraic is empty.

Negative integers are both negative and integers.

 $\mathbb{Z}^- = \mathbb{Z} \cap \mathbb{R}^-$

All integers are rational numbers.

 $\mathbb{Z} \in \mathbb{R}$

Since all rational numbers are algebraic numbers and all algebraic numbers are real numbers, it follows that all rational numbers are real num- $\therefore \mathbb{Q} \subseteq \mathbb{R}$ bers.

 $\mathbb{Q} \subseteq \mathbb{A}$ $\mathbb{A}\subseteq\mathbb{R}$

Axiom (Existence.)

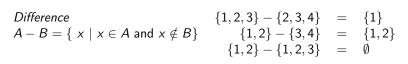
There is a set with no elements.

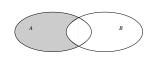
Axiom (Extensionality.)

If every element of a set X is an element of a set Y and every element of Y is an element of X, then X = Y.

Union
$$\{1,2,3\} \cup \{2,3,4\} = \{1,2,3,4\}$$
 $A \cup B = \{x \mid x \in A \text{ or } x \in B\}$ $\{1,2\} \cup \{3,4\} = \{1,2,3,4\}$ $\{1,2\} \cup \{1,2,3\} = \{1,2,3\}$

Intersection
$$\{1,2,3\} \cap \{2,3,4\} = \{2,3\}$$
 $A \cap B = \{x \mid x \in A \text{ and } x \in B\}$ $\{1,2\} \cap \{3,4\} = \emptyset$ $\{1,2\} \cap \{1,2,3\} = \{1,2\}$



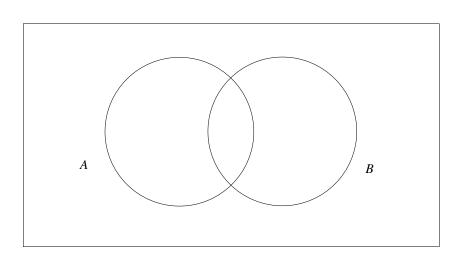


1.
$$\{1,2,3,4,5\} \cup \{5,6,7\} =$$

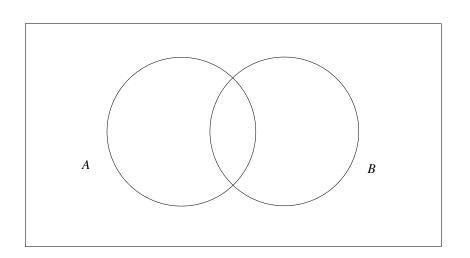
2.
$$\{1, 2, 3, 4, 5\} \cap \{2, 4, 6, 8, 10\} =$$

3.
$$\{1, 2, 3, 4, 5\} - \{2, 3, 4\} =$$

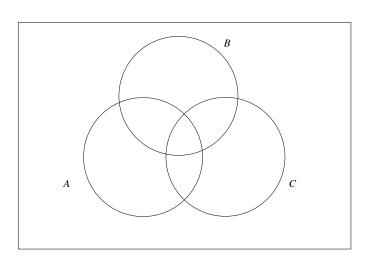
4.
$$\{1,2,3,4,5\} - \{3,4,5,6,7\} =$$



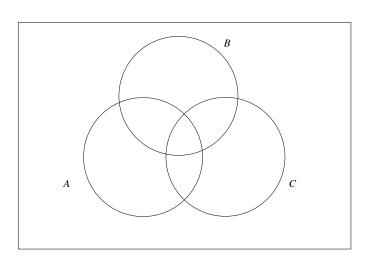
1.4.7. $(A \cap B) - A$



1.4.8.
$$(A - B) \cup (B - A)$$



1.4.9. $(A \cup B) \cap (A \cup C)$



1.4.10. $\overline{(A \cap B)} \cap (A \cup C)$

(Exercises 1.4.(11–18).)

$$-12 \in \mathbb{R}^-$$
.

$$\mathbb{Q} \cap \mathbb{T} = \emptyset$$
.

$$\mathbb{A}\subseteq\mathbb{C}.$$

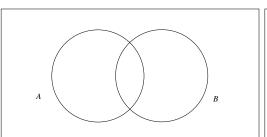
$$\frac{1}{63} \in \mathbb{Q} - \mathbb{R}$$
.

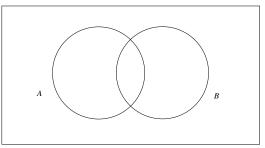
$$\mathbb{R}\subseteq\mathbb{C}\cap\mathbb{R}^-$$

$$\mathbb{Z} - \mathbb{R}^- = \mathbb{W}$$
.

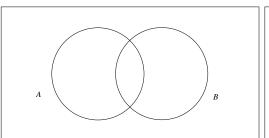
$$4\in\mathbb{C}.$$

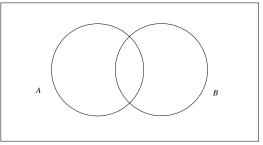
$$\mathbb{T} \cup \mathbb{Z} \subseteq \mathbb{A}.$$



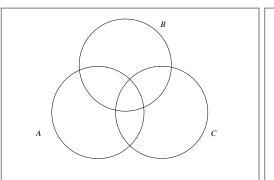


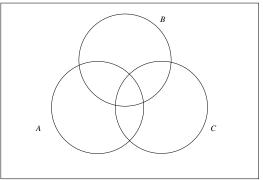
$$A \cup (A \cap B) = A$$



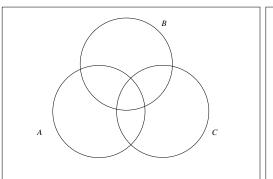


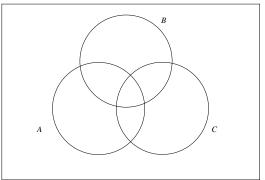
$$A \cup \overline{A} = \mathcal{U}$$



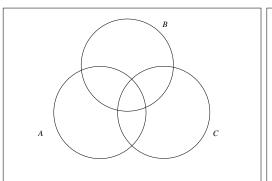


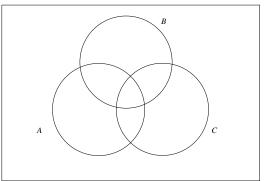
$$A \cup (B \cup C) = (A \cup B) \cup C$$



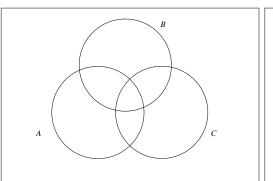


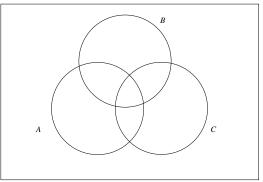
$$A\cap (B\cup C)=(A\cap B)\cup (A\cap C)$$



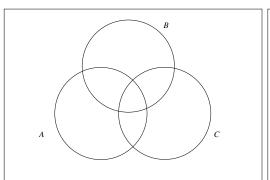


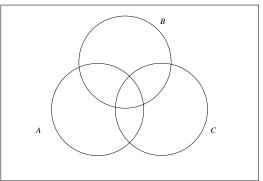
$$A \cap B = A - (A - B)$$



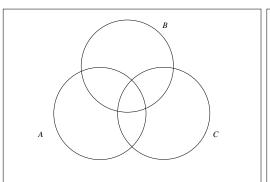


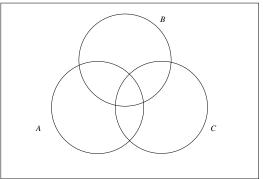
$$(A \cap C) - (C - B) = A \cap B \cap C$$





$$A \cup (A - B) = A$$





$$(A \cup (B - C)) \cap \overline{B} = A - B$$

For next time:

Pg 12: 1.3.(11-14, 16)

Pg 16: 1.4.(1-6, 19)

Pg 20: 1.5.(8-11)

Remember, submit through Schoology (as a PDF).

Read 1.(6-9)

Take quiz