

Division method:

$$h(k) = k \mod m$$

Middle square method (see code)

Multiplicative method:

$$h(k) = \lfloor m(k \cdot a - \lfloor k \cdot a \rfloor) \rfloor$$

“Universal” hash (next time)

ASCII sum:

$$h(k) = \left( \sum_{i=0}^{n-1} s[i] \right)$$

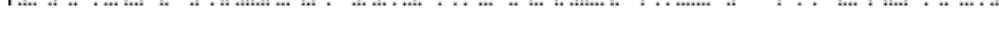
String polynomial:

$$h(k) = (k[0] \cdot b^{n-1} + k[1] \cdot b^{n-2} + \cdots + k[n-2] \cdot b + k[n-1]) \mod m$$

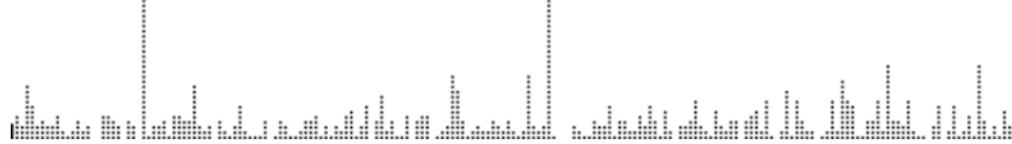
Carter-Wegman:

$$\begin{aligned} h(k) &= (h_0(k[0]) + h_1(k[1]) + \cdots + h_{n-1}(k[n-1])) \mod m \\ &= \left( \sum_{i=0}^{n-1} h_i(k[i]) \right) \mod m \end{aligned}$$

		Average penalty	Variance
<b>Area codes (<math>n = 303</math>)</b>			
Division		.673	.808
Mid square		1.09	1.64
Multiplicative		.508	.478
Fibonacci		.617	.696
Universal		.578	.617
<b>Book ISBNs (<math>n = 718</math>)</b>			
Division		.618	1.05
Mid square		.812	1.48
Multiplicative		.565	.954
Fibonacci		.544	.873
Universal		.667	1.15

		Average penalty	Variance
Randomly generated from [0, 1000) ( $n = 150$ )			
Division		1.36	.958
Mid square		1.86	1.96
Multiplicative		1.34	.919
Fibonacci		1.41	1.07
Universal		1.39	1.02

		Average penalty	Variance
Randomly generated from [0, 1000) ( $n = 400$ )			
Division		.518	1.16
Mid square		1.73	3.68
Multiplicative		.405	.930
Fibonacci		.448	.980
Universal		.488	1.08

		Average penalty	Variance
Chemicals ( $n = 663$ )			
ASCII sum		.505	1.00
String polynomial		.424	.805
Carter-Wegman		.800	1.63
Books ( $n = 718$ )			
ASCII sum		.818	1.51
String polynomial		.745	1.30
Carter-Wegman		2.06	4.08

		Average penalty	Variance
Randomly generated strings ( $n = 150$ )			
ASCII sum	.....	1.32	.879
String polynomial	.....	1.43	1.09
Carter-Wegman	.....	1.41	1.05

Randomly generated strings ( $n = 400$ )

ASCII sum	.....	.515	1.15
String polynomial	.....	.425	.925
Carter-Wegman	.....	.540	1.20