

Backpropagation

Initialize all weights in all units to random value

Repeat until termination condition

For each data point \mathbf{x}_i, t_i

Compute z_k and y_ℓ for every unit in the network

For each output unit y_ℓ

$$\delta_{y_\ell} = y_\ell(\mathbf{x}_i)(1 - y_\ell(\mathbf{x}_i))(t_i - y_\ell(\mathbf{x}_i))$$

For each hidden unit z_k

$$\delta_{z_k} = z_k(\mathbf{x}_i)(1 - z_k(\mathbf{x}_i)) \sum_{\ell=1}^K w_{\ell k} \delta_{y_\ell}$$

For each output unit y_ℓ

For each weight $w_{y_\ell k}$

$$w_{y_\ell k} + = \eta \delta_{y_\ell} z_k(\mathbf{x}_i)$$

For each hidden unit z_k

For each weight $w_{z_k j}$

$$w_{z_k j} + = \eta \delta_{z_k} x_{ij}$$

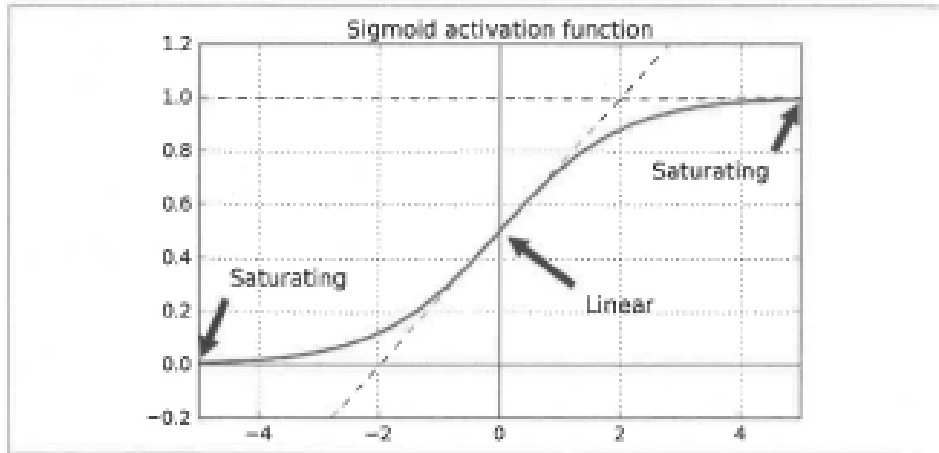


Figure 11-1. Logistic activation function saturation

Aurélien Géron, *Hands-On Machine Learning with Scikit-Learn & TensorFlow*, O'Reilly, 2017. Pg 279.

Table 11-1. Initialization parameters for each type of activation function

Activation function	Uniform distribution $[-r, r]$	Normal distribution
Logistic	$r = \sqrt{\frac{6}{n_{\text{inputs}} + n_{\text{outputs}}}}$	$\sigma = \sqrt{\frac{2}{n_{\text{inputs}} + n_{\text{outputs}}}}$
Hyperbolic tangent	$r = 4\sqrt{\frac{6}{n_{\text{inputs}} + n_{\text{outputs}}}}$	$\sigma = 4\sqrt{\frac{2}{n_{\text{inputs}} + n_{\text{outputs}}}}$
ReLU (and its variants)	$r = \sqrt{2}\sqrt{\frac{6}{n_{\text{inputs}} + n_{\text{outputs}}}}$	$\sigma = \sqrt{2}\sqrt{\frac{2}{n_{\text{inputs}} + n_{\text{outputs}}}}$

Aurélien Géron, *Hands-On Machine Learning with Scikit-Learn & TensorFlow*, O'Reilly, 2017. Pg 280.

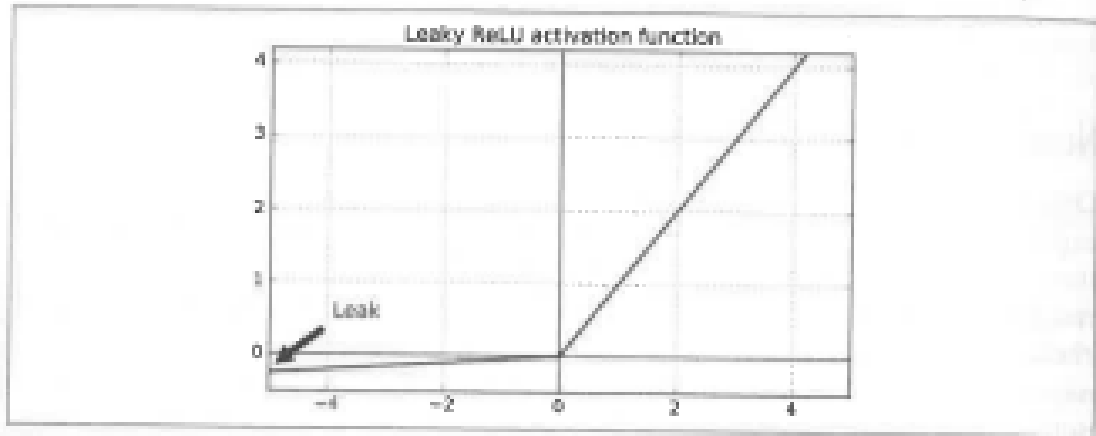


Figure 11-2. Leaky ReLU

Aurélien Géron, *Hands-On Machine Learning with Scikit-Learn & TensorFlow*, O'Reilly, 2017. Pg 282.

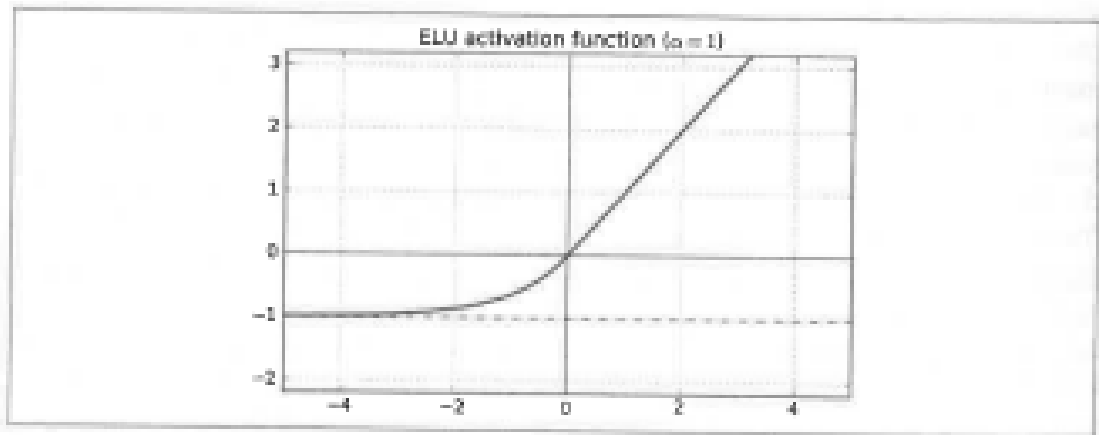


Figure 11-3. ELU activation function

Aurélien Géron, *Hands-On Machine Learning with Scikit-Learn & TensorFlow*, O'Reilly, 2017. Pg 282.