

A **proposition** is a sentence that is true or false, but not both.

It is snowing and it is not Thursday.

A **propositional form** is like a proposition but with content replaced by variables.

p and not q

$p \wedge \sim q$

$$\mathbb{Z} = \{\dots - 3, -2, -1, 0, 1, 2, 3 \dots\}$$

$+ - \times \div$

\times	0	1	2	3
0	0	0	0	0
1	0	1	2	3
2	0	2	4	6
3	0	3	6	9

$$\mathbb{B} = \{T, F\}$$

$\vee \wedge \sim$

\wedge	T	F
T	T	F
F	F	F

p	$\sim p$
T	F
F	T

\wedge	T	F
T	T	F
F	F	F

\vee	T	F
T	T	T
F	T	F

p	q	$p \wedge q$
T	T	T
T	F	F
F	T	F
F	F	F

p	q	$p \vee q$
T	T	T
T	F	T
F	T	T
F	F	F

p	q	$p \wedge q$	$p \vee q$	$\sim p$
T	T	T	T	F
T	F	F	T	F
F	T	F	T	T
F	F	F	F	T

p	q	$\sim p$	$\sim q$	$p \wedge q$	$\sim (p \wedge q)$	$\sim p \vee \sim q$
T	T	F	F	T	F	F
T	F	F	T	F	T	T
F	T	T	F	F	T	T
F	F	T	T	F	T	T

Commutative laws:

$$p \wedge q \equiv q \wedge p$$

$$p \vee q \equiv q \vee p$$

Associative laws:

$$(p \wedge q) \wedge r \equiv p \wedge (q \wedge r)$$

$$(p \vee q) \vee r \equiv p \vee (q \vee r)$$

Distributive laws:

$$p \wedge (q \vee r) \equiv (p \wedge q) \vee (p \wedge r)$$

$$p \vee (q \wedge r) \equiv (p \vee q) \wedge (p \vee r)$$

Absorption laws:

$$p \wedge (p \vee q) \equiv p$$

$$p \vee (p \wedge q) \equiv p$$

Idempotent laws:

$$p \wedge p \equiv p$$

$$p \vee p \equiv p$$

Double negative law:

$$\sim \sim p \equiv p$$

DeMorgan's laws:

$$\sim (p \wedge q) \equiv \sim p \vee \sim q$$

$$\sim (p \vee q) \equiv \sim p \wedge \sim q$$

Negation laws:

$$p \vee \sim p \equiv T$$

$$p \wedge \sim p \equiv F$$

Universal bound laws:

$$p \vee T \equiv T$$

$$p \wedge F \equiv F$$

Identity laws:

$$p \wedge T \equiv p$$

$$p \vee F \equiv p$$

Tautology and contradiction laws:

$$\sim T \equiv F$$

$$\sim F \equiv T$$