

Chapter 6, Hash tables:

- ▶ General introduction; separate chaining (last Friday)
- ▶ Open addressing (Monday)
- ▶ Hash functions (**Today**)
- ▶ Perfect hashing (next week Monday)
- ▶ Hash table performance (next week Wednesday)

Today:

- ▶ Hash function properties
- ▶ Integer hashes
- ▶ String hashes
- ▶ Experimental results

Hash functions should distribute the keys *uniformly* and *independently*.

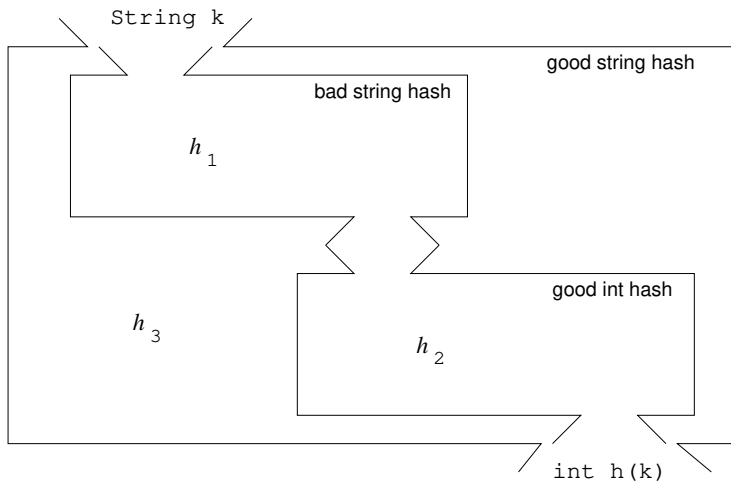
Uniformity:

$$P(h(k) = i) = \frac{1}{m}$$

Independence:

$$P(h(k_1) = i) = P(h(k_1) = i \mid h(k_2) = j)$$

Why do we talk about integer hashes?



Division method:

$$h(k) = k \bmod m$$

Middle square method (see code)

Multiplicative method:

$$h(k) = \lfloor m(k \cdot a - \lfloor k \cdot a \rfloor) \rfloor$$

“Universal” hash (next time)

ASCII sum:

$$h(k) = \left(\sum_{i=0}^{n-1} s[i] \right)$$

String polynomial:




$$h(k) = (k[0] \cdot b^{n-1} + k[1] \cdot b^{n-2} + \dots + k[n-2] \cdot b + k[n-1]) \pmod{m}$$

Carter-Wegman:

$$\begin{aligned} h(k) &= (h_0(k[0]) + h_1(k[1]) + \dots + h_{n-1}(k[n-1])) \pmod{m} \\ &= \left(\sum_{i=0}^{n-1} h_i(k[i]) \right) \pmod{m} \end{aligned}$$



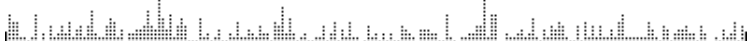


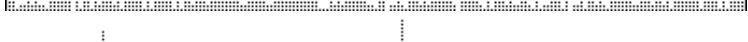
		Average penalty	Variance
Area codes ($n = 303$)			
Division		.673	.808
Mid square		1.09	1.64
Multiplicative		.508	.478
Fibonacci		.617	.696
Universal		.578	.617

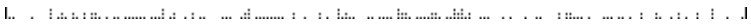

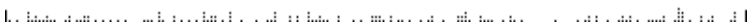
Book ISBNs ($n = 718$)

Division		.618	1.05
Mid square		.812	1.48
Multiplicative		.565	.954
Fibonacci		.544	.873
Universal		.667	1.15

		Average penalty	Variance
Randomly generated from [0, 1000) ($n = 150$)			
Division		1.36	.958
Mid square		1.86	1.96
Multiplicative		1.34	.919
Fibonacci		1.41	1.07
Universal		1.39	1.02

Randomly generated from [0, 1000) ($n = 400$)			
Division		.518	1.16
Mid square		1.73	3.68
Multiplicative		.405	.930
Fibonacci		.448	.980
Universal		.488	1.08

		Average penalty	Variance
Chemicals ($n = 663$)			
ASCII sum		.505	1.00
String polynomial		.424	.805
Carter-Wegman		.800	1.63
Books ($n = 718$)			
ASCII sum		.818	1.51
String polynomial		.745	1.30
Carter-Wegman		2.06	4.08

Randomly generated strings ($n = 150$)		Average penalty	Variance
ASCII sum		1.32	.879
String polynomial		1.43	1.09
Carter-Wegman		1.41	1.05

Randomly generated strings ($n = 400$)

ASCII sum		.515	1.15
String polynomial		.425	.925
Carter-Wegman		.540	1.20

Coming up:

Do **Open Addressing Hashtable** project (*suggested by Monday, Apr 18*)

Due Mon, Apr 18

Read Sections 7.(4 & 5)

(No practice problems or quiz)

Due Thurs, Apr 21 (*end of day*)

Read Section 7.6

Take quiz