Chapter 1 outline:

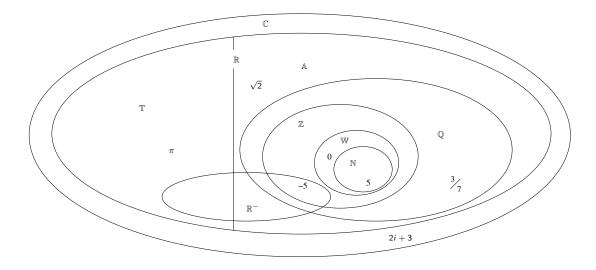
- Introduction, sets and elements (this past Monday)
- Set operations; visual verification of set propositions (Today)
- Introduction to SML; cardinality and Cartesian products (Friday)

▲□▶ ▲□▶ ▲□▶ ▲□▶ ■ ●の00

- Making types in SML (next week Wednesday)
- Making functions in SML (next week Friday)

Today:

- Set symbols and terminology
- Set notation
- Set operations
- Verifying set equivalence visually



・ロト・雪 ・ モー・ モー・ つんの

5 is a natural number; or the collection of natural numbers contains 5. $5 \in \mathbb{N}$

Adding 0 to the collection of natural numbers makes the collection of $\mathbb{N} \cup \{0\} = \mathbb{W}$ whole numbers.

Merging the algebraic numbers and the transcendental numbers makes $A \cup T = \mathbb{R}$ the real numbers.

Transcendental numbers are those real numbers which are not algebraic $~~\mathbb{T}=\mathbb{R}-\mathbb{A}$ numbers.

Nothing is both transcendental and algebraic, *or* the collection of things $\mathbb{T} \cap \mathbb{A} = \emptyset$ both transcendental and algebraic is empty.

Negative integers are both negative and integers. $\mathbb{Z}^- = \mathbb{Z} \cap \mathbb{R}^-$

All integers are rational numbers. $\mathbb{Z} \in \mathbb{R}$

Since all rational numbers are algebraic numbers and all algebraic numbers are real numbers, it follows that all rational numbers are real numbers. $\mathbb{Q} \subseteq \mathbb{R}$ bers.

・ロト < 団ト < 三ト < 三ト < 三 ・ のへで

 $\mathbb{Q} \subseteq \mathbb{A}$

Axiom (Existence.)

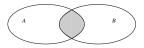
There is a set with no elements.

Axiom (Extensionality.)

If every element of a set X is an element of a set Y and every element of Y is an element of X, then X = Y.

▲□▶▲□▶▲≡▶▲≡▶ ≡ めぬる

Intersection
$$\{1,2,3\} \cap \{2,3,4\}$$
= $\{2,3\}$ $A \cap B = \{ x \mid x \in A \text{ and } x \in B \}$ $\{1,2\} \cap \{3,4\}$ = \emptyset $\{1,2\} \cap \{1,2,3\}$ = $\{1,2\}$



Difference	$\{1,2,3\}-\{2,3,4\}$	=	$\{1\}$	
$A - B = \{ x \mid x \in A \text{ and } x \notin B \}$	$\{1,2\}-\{3,4\}$	=	$\{1, 2\}$	
	$\{1,2\}-\{1,2,3\}$	=	Ø	

1.
$$\{1, 2, 3, 4, 5\} \cup \{5, 6, 7\} =$$

2.
$$\{1, 2, 3, 4, 5\} \cap \{2, 4, 6, 8, 10\} =$$

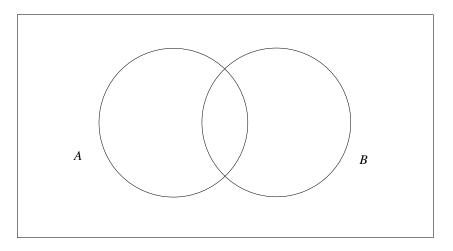
3.
$$\{1, 2, 3, 4, 5\} - \{2, 3, 4\} =$$

4.
$$\{1, 2, 3, 4, 5\} - \{3, 4, 5, 6, 7\} =$$

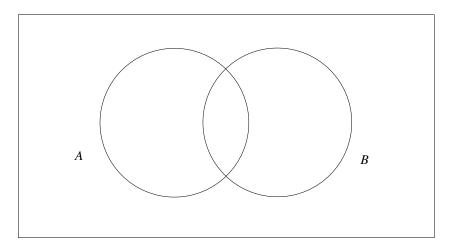
Which of the following are equal to $\{1, 2, 3, 4\}$?

- ▶ ${1,2} \cup {3,4}$
- ▶ ${1, 2, 3} \cup {4}$
- ▶ ${1,2,3} \cup {2,3,4}$
- ▶ ${1,2,3} \cup {3,4,5}$
- ▶ ${2,3} \cup {1,4}$
- ▶ ${1} \cup {3,4}$
- ▶ {4, 3, 2, 1}
- $\blacktriangleright \ \{1\} \cup \{1,2\} \cup \{1,2,3\} \cup \{1,2,3,4\}$

▲ロ ▶ ▲周 ▶ ▲ 国 ▶ ▲ 国 ▶ ● の Q @

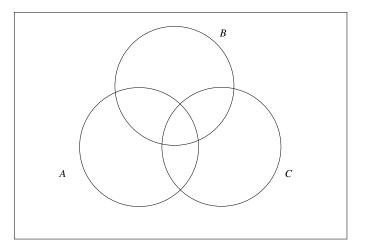


1.4.7. $(A \cap B) - A$



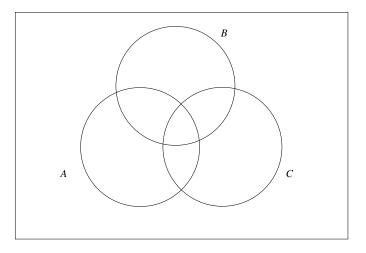
◆□ > ◆□ > ◆ 三 > ◆ 三 > ● ○ ○ ○ ○

1.4.8. $(A - B) \cup (B - A)$

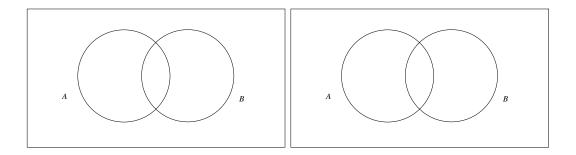


◆□ > ◆□ > ◆ 三 > ◆ 三 > ● ○ ○ ○ ○

1.4.9. $(A \cup B) \cap (A \cup C)$

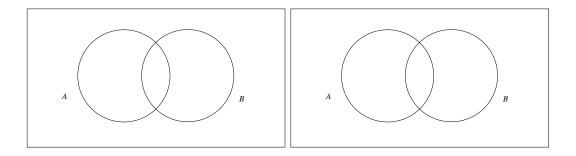


1.4.10. $\overline{(A \cap B)} \cap (A \cup C)$



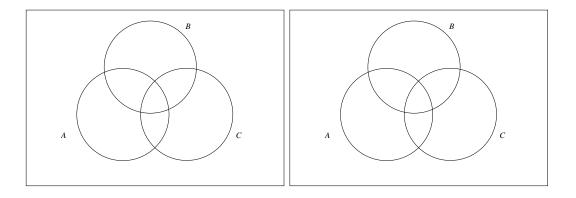
 $A\cup (A\cap B)=A$

▲□▶ ▲□▶ ▲ □▶ ▲ □▶ ▲ □ ● ● ● ●



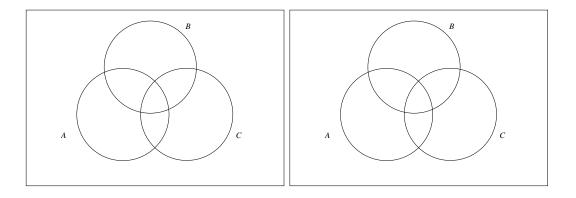
 $A \cup \overline{A} = \mathcal{U}$

▲□▶ ▲□▶ ▲ 三▶ ▲ 三 ● ● ●



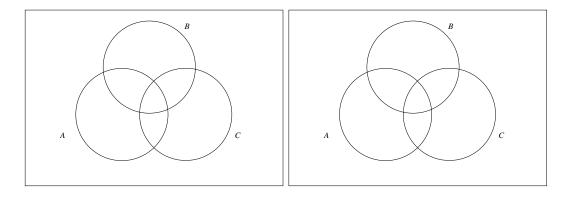
$$A \cup (B \cup C) = (A \cup B) \cup C$$

▲ロト ▲圖 ▶ ▲目 ▶ ▲目 ▶ ▲目 ● ● ● ●

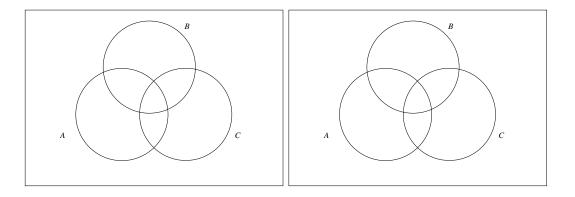


 $A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$

◆□▶ ◆□▶ ◆三▶ ◆三▶ 三三 - のへで

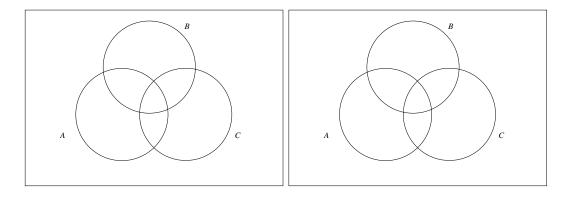


$$A \cap B = A - (A - B)$$



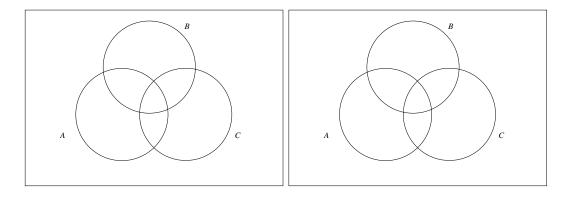
$$(A \cap C) - (C - B) = A \cap B \cap C$$

▲ロト ▲圖 ▶ ▲目 ▶ ▲目 ▶ ▲目 ● ● ● ●



$$A \cup (A - B) = A$$

|▲□▶ ▲圖▶ ▲臣▶ ▲臣▶ | 臣|||のへで



$$(A \cup (B - C)) \cap \overline{B} = A - B$$

For next time:

Pg 12: 1.3.(11-14, 16) Pg 16: 1.4.(1-6, 19) Pg 20: 1.5.(8-11) Read 1.(6-9) Take quiz

◆□ ▶ ◆□ ▶ ◆ □ ▶ ◆ □ ▶ ○ □ ○ ○ ○ ○