## Chapter 6, Hash tables:

- General introduction; separate chaining (last week Friday)
- Open addressing (Today)
- Hash functions (Friday)
- Perfect hashing (next week Monday)
- Hash table performance (next week Wednesday)

## Today:

- ► Review/finish hash table concepts
- Basic idea and example of open addressing
- ► Terminology, code, and invariant
- Probing strategies
- Deletion

Hash functions should distribute the keys uniformly and independently.

Uniformity:

$$P(h(k)=i)=\frac{1}{m}$$

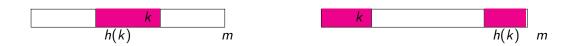
Independence:

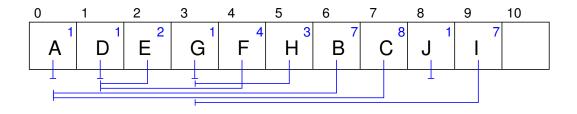
$$P(h(k_1) = i) = P(h(k_1) = i \mid h(k_2) = j)$$

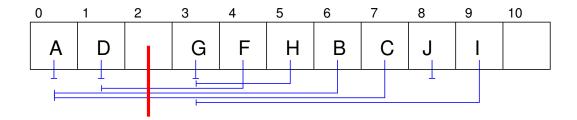
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
|---|---|---|---|---|---|---|---|---|---|----|----|----|

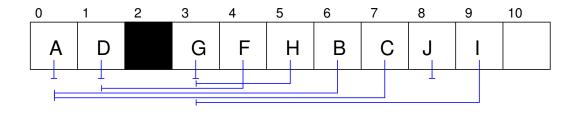
# Invariant (Class OpenAddressingHashMap)

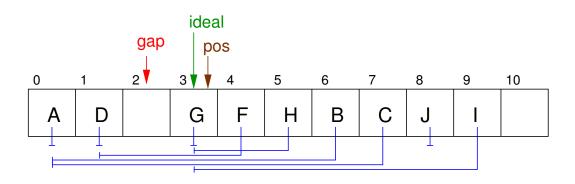
- 1. The table it not full; there exists  $i \in [0, m)$  such that table [i] = null.
- 2. There are no breaks in the chain for any key in the table; for all  $i \in [0, m)$  such that table[i] contains key k,
  - ▶ if  $h(k) \le i$ , then for all  $j \in [h(k), i]$ , table $[j] \ne \text{null}$ ;
  - ▶ if i < h(k), then for all  $j \in [0, i] \cup [h(k), m)$ , table  $[j] \neq \text{null}$ .

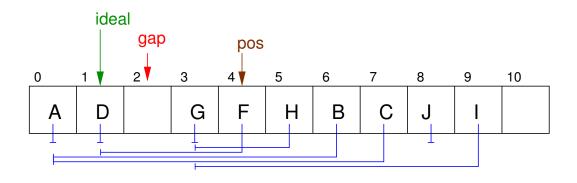


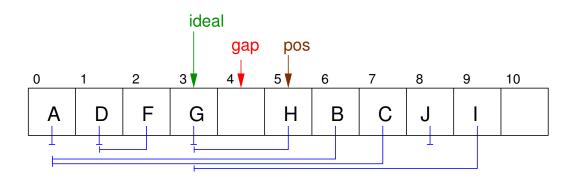


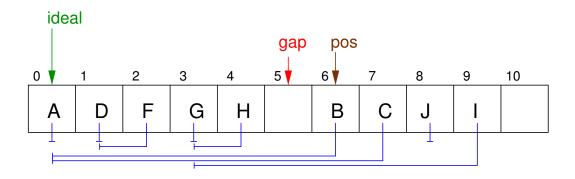


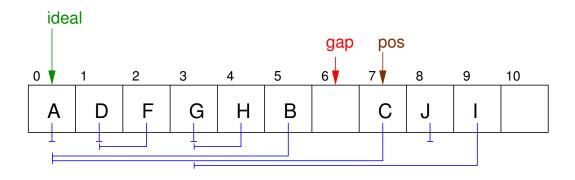


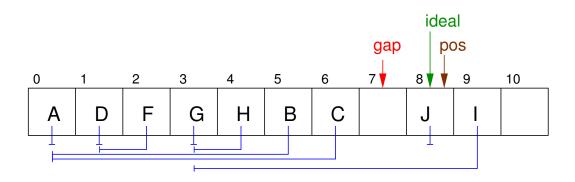


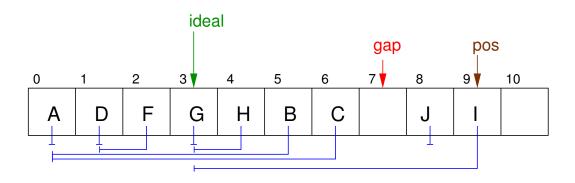


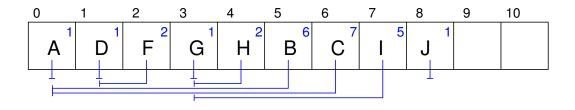




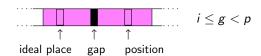


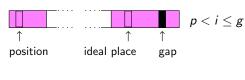




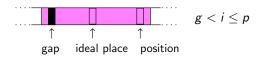


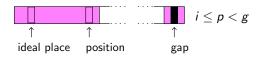
#### Cases to plug the gap

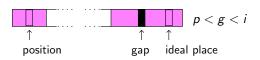




### Cases to skip the gap







## Invariant (Loop of optimized remove in linear probing.)

For all positions  $k \in (i,j)$ , gap is the only position, if any, between its ideal place (h(keys[k])) and its actual place (k).

Coming up: (all end-of-day)

Do Optimal BST project (due this past Monday, April 8)
Do Open addressing with linear probing project (due Monday, Apr 15)

Due **Thurs Apr 11**Read Section 7.3
Do Exercises 7.(4,5,7,8)
Take quiz

Due Mon, Apr 15
Read Sections 7.(4 & 5)
(No practice problems or quiz)